



# Computing Performance when Solving Routing Problems: From Python to Julia

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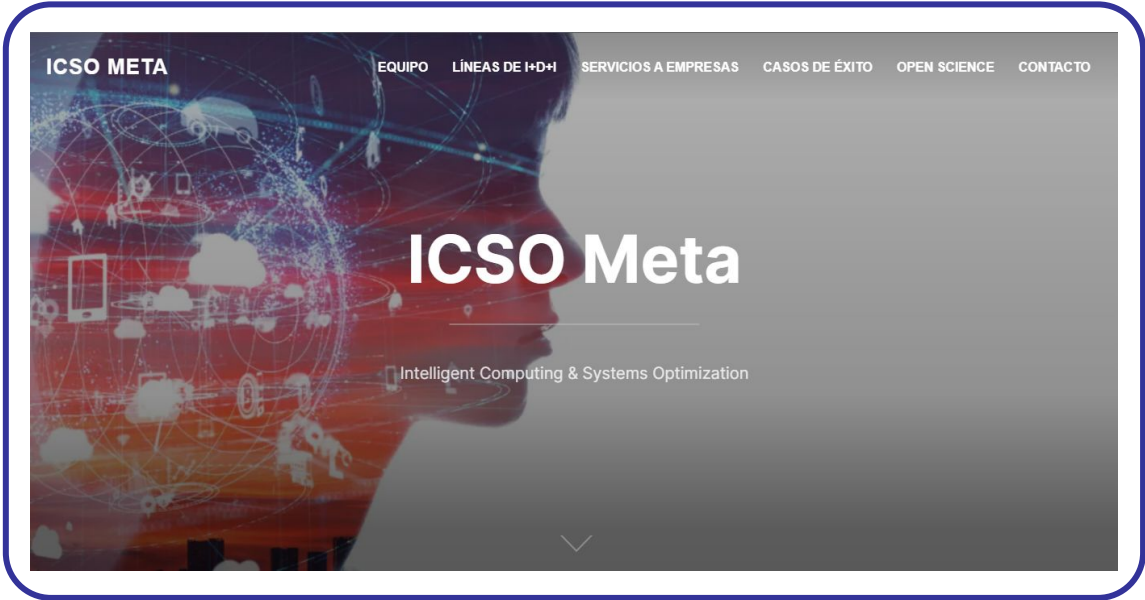
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**Part I:**  
**Introduction**

# ICSO Meta

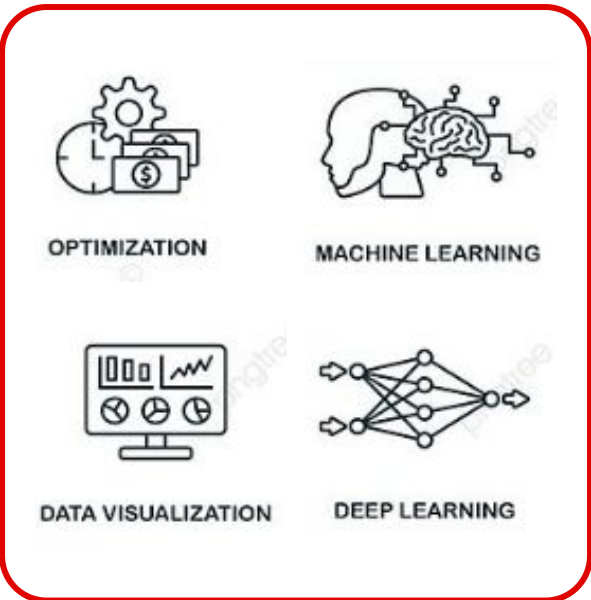


ICSO META

EQUIPO LÍNEAS DE I+D+i SERVICIOS A EMPRESAS CASOS DE ÉXITO OPEN SCIENCE CONTACTO

## ICSO Meta

Intelligent Computing & Systems Optimization

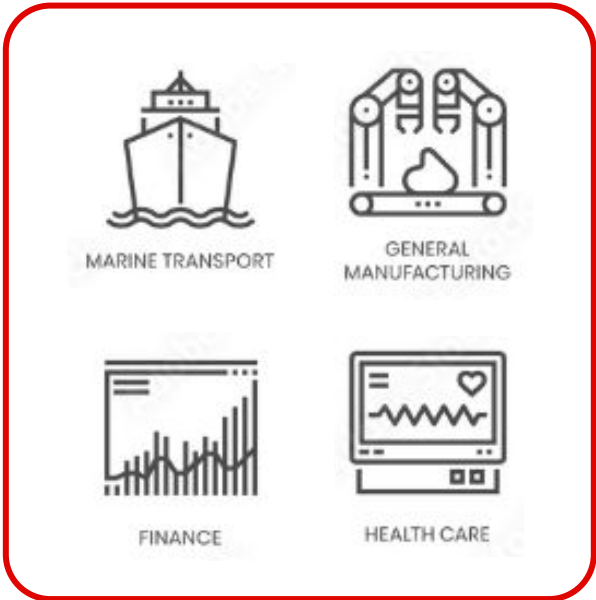


OPTIMIZATION

MACHINE LEARNING

DATA VISUALIZATION

DEEP LEARNING



MARINE TRANSPORT

GENERAL MANUFACTURING

FINANCE

HEALTH CARE



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# Programming Language History



- **Powerful computational capabilities**
- **Challenging to use for non-computer science experts**

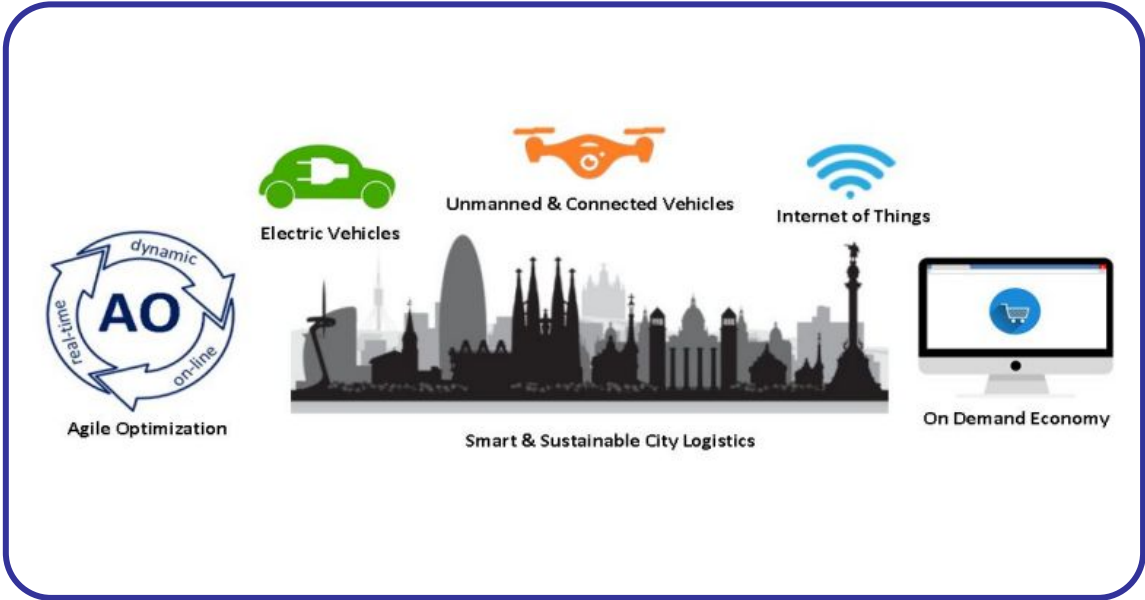


- **Gentle learning curve**
- **Great accessibility for non-computer science experts**
- **Extensive environment and libraries**



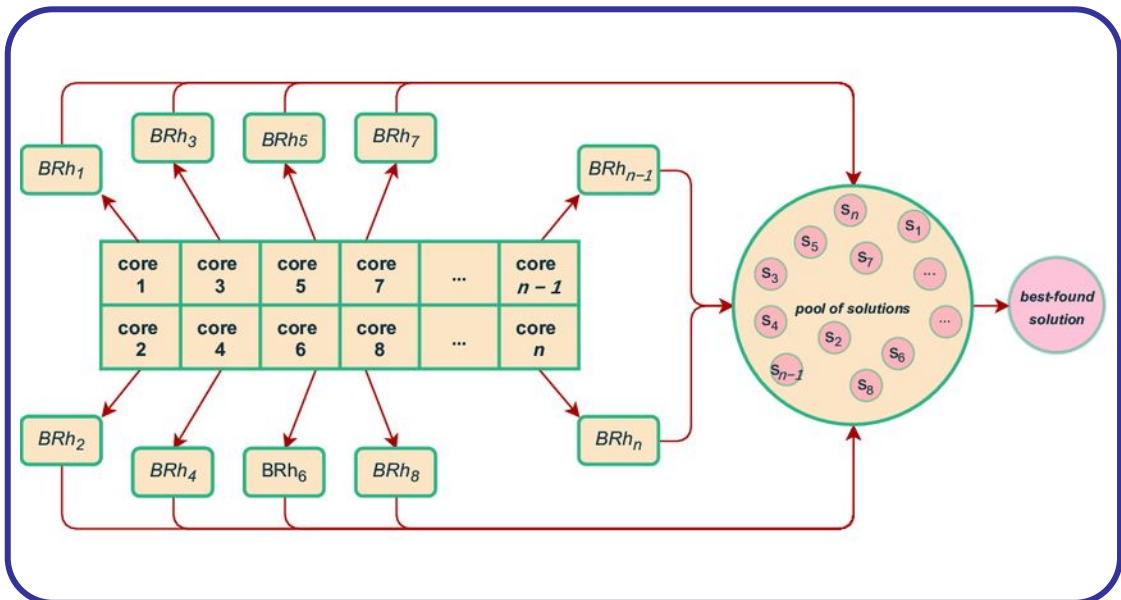
- **High-performance language for scientific computing**
- **Exceptional speed and innate support for parallel computing**

# Motivation



- Adapt to **real-world scenarios**
- Conditions of an optimization problem are **dynamic** and can **change over time**

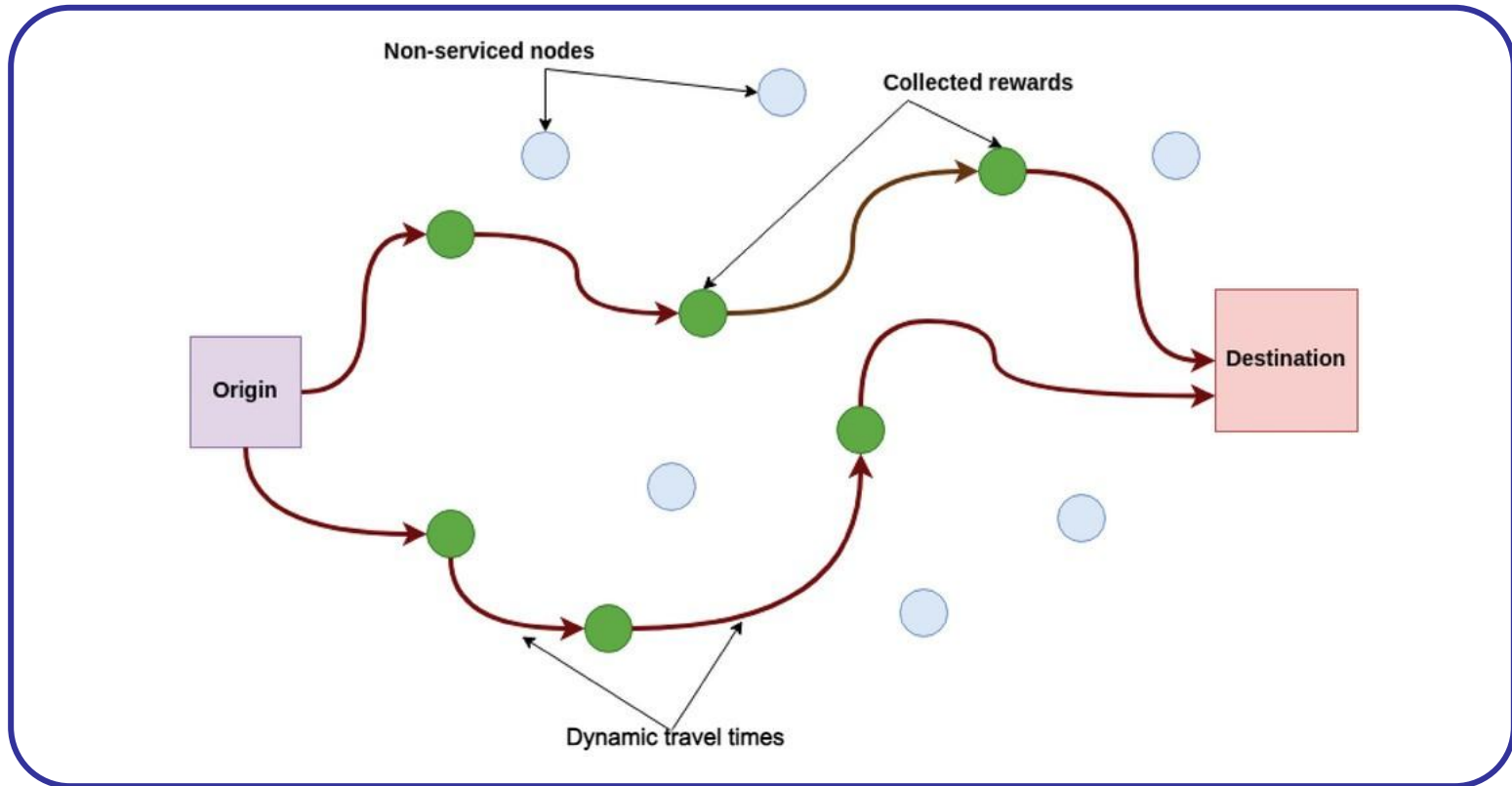
- Solved by **'agile' optimization algorithms**
- The relevance of dynamism gives importance to **performance, efficiency, and responsiveness**



**Part II:**

**Solving Routing Problems**

# The Team Orienteering Problem



- Essential problem in **logistics and transportation**, which finds applications across **many industries**
- Among the real-world applications we can find **public transport, waste collection, carsharing, and ridesharing** among others

# The Python Approach (I)

```
class Node:
```

```
    def __init__(self, ID, x, y, reward):
        self.ID = ID
        self.x = x
        self.y = y
        self.reward = reward
        self.dnEdge = None
        self.ndEdge = None
        self.inRoute = None
        self.isLinkedToStart = False
        self.isLindedToFinish = False
```

```
class Edge:
```

```
    def __init__(self, origin, end):
        self.origin = origin
        self.end = end
        self.cost = 0.0
        self.savings = 0.0
        self.efficiency = 0.0
        self.invEdge = None
```

```
class Route:
```

```
    def __init__(self):
        self.edges = []
        self.cost = 0.0
        self.reward = 0.0
```

```
...
```

- **Simple POD types in OOP style**
- **Dynamic typing with default values**

# The Python Approach (II)

```
def PJS_Heuristic(inputs, test, efficiencyList, isRand, rng):  
    # Construct a dummy solution  
    solution = genDummySolution(inputs)  
    effList = efficiencyList.copy()  
  
    while len(effList) > 0:  
        # Select ijEdge from the savings list  
        pos = getRandPos(test.betaMin, test.betaMax, len(effList), rng) if isRand else 0  
        ijEdge = effList.pop(pos)  
  
        # Determine nodes and routes of ijEdge  
        iNode = ijEdge.origin  
        jNode = ijEdge.end  
        iRoute = iNode.inRoute  
        jRoute = jNode.inRoute  
  
        # If conditions are satisfied, merge routes and delete edge  
        if isMergePossible(iNode, jNode, iRoute, jRoute, ijEdge, inputs.Tmax):  
            jiEdge = ijEdge.invEdge  
            if jiEdge in effList:  
                effList.remove(jiEdge)  
  
            # Remove iEdge from iRoute  
            iEdge = iRoute.edges[-1]  
            iRoute.edges.remove(iEdge)  
            iRoute.cost -= iEdge.cost  
            iNode.isLinkedToFinish = False  
  
            # Remove jEdge from jRoute  
            jEdge = jRoute.edges[0]  
            jRoute.edges.remove(jEdge)  
            jRoute.cost -= jEdge.cost  
            jNode.isLinkedToStart = False
```

- **Automatic memory management**
- **Use of built-in types methods for logic operations (OOP)**

# The Julia Approach (I)

```
abstract type AbstractEdge end
abstract type AbstractRoute end
```

```
mutable struct Node
```

```
    id :: Int64
    x :: Float64
    y :: Float64
    reward :: Float64
    dnEdge :: Union{Nothing, AbstractEdge} = nothing
    ndEdge :: Union{Nothing, AbstractEdge} = nothing
    inRoute :: Union{Nothing, AbstractRoute} = nothing
    isInterior :: Bool = false
    isLinkedToStart :: Bool = false
    isLinkedToFinish :: Bool = false
```

```
end
```

```
mutable struct Edge <: AbstractEdge
```

```
    origin :: Node
    finish :: Node
    cost :: Float64 = 0.0
    savings :: Float64 = 0.0
    efficiency :: Float64 = 0.0
    invEdge :: Union{Nothing, AbstractEdge} = nothing
```

```
end
```

```
mutable struct Route <: AbstractRoute
```

```
    edges :: Vector{Edge} = []
    cost :: Float64 = 0.0
    reward :: Float64 = 0.0
```

```
end
```

```
...
```

- **Simple POD types in procedural style.**
- **Static typing with default values**

# The Julia Approach (II)

```
function PJS_Heuristic(inputs, test, nodes, efficiencyList, isRand, rng)
    # Construct a dummy solution
    solution = genDummySolution(nodes, inputs.Tmax)
    effList = copy(efficiencyList)

    while length(effList) > 0
        # Select ijEdge from the savings list
        pos = isRand ? getRandPos(test.betaMin, test.betaMax, length(effList), rng) : 1
        ijEdge = popat!(effList, pos)

        # Determine nodes and routes of ijEdge
        iNode = ijEdge.origin
        jNode = ijEdge.finish
        iRoute = iNode.inRoute
        jRoute = jNode.inRoute

        # If conditions are satisfied, merge routes and delete edge
        if isMergeFeasible(iNode, jNode, iRoute, jRoute, ijEdge, inputs.Tmax)
            jiEdge = ijEdge.invEdge
            if jiEdge in effList
                remove!(effList, jiEdge)
            end

            # Remove iEdge from iRoute
            iEdge = iRoute.edges[-1]
            remove!(iRoute.edges, iEdge)
            iRoute.cost -= iEdge.cost
            iNode.isLinkedToFinish = false

            # Remove jEdge from jRoute
            jEdge = jRoute.edges[1]
            remove!(jRoute.edges, jEdge)
            jRoute.cost -= jEdge.cost
            jNode.isLinkedToStart = false
        end
    end
end
```

- **Automatic memory management**
- **Use of free functions for logic operations (procedural)**

# **Part II:**

# **Computing Performance**

# Benchmark Process (I)

- Our **benchmark process** was comprehensive, testing the implementations with instances from **Chao et. al (1996)**
- For each instance, we conducted **1000 runs** of each algorithm, meticulously **collecting essential statistics**
- This included calculating the **mean execution time**, and tracking the **maximum and minimum execution times**

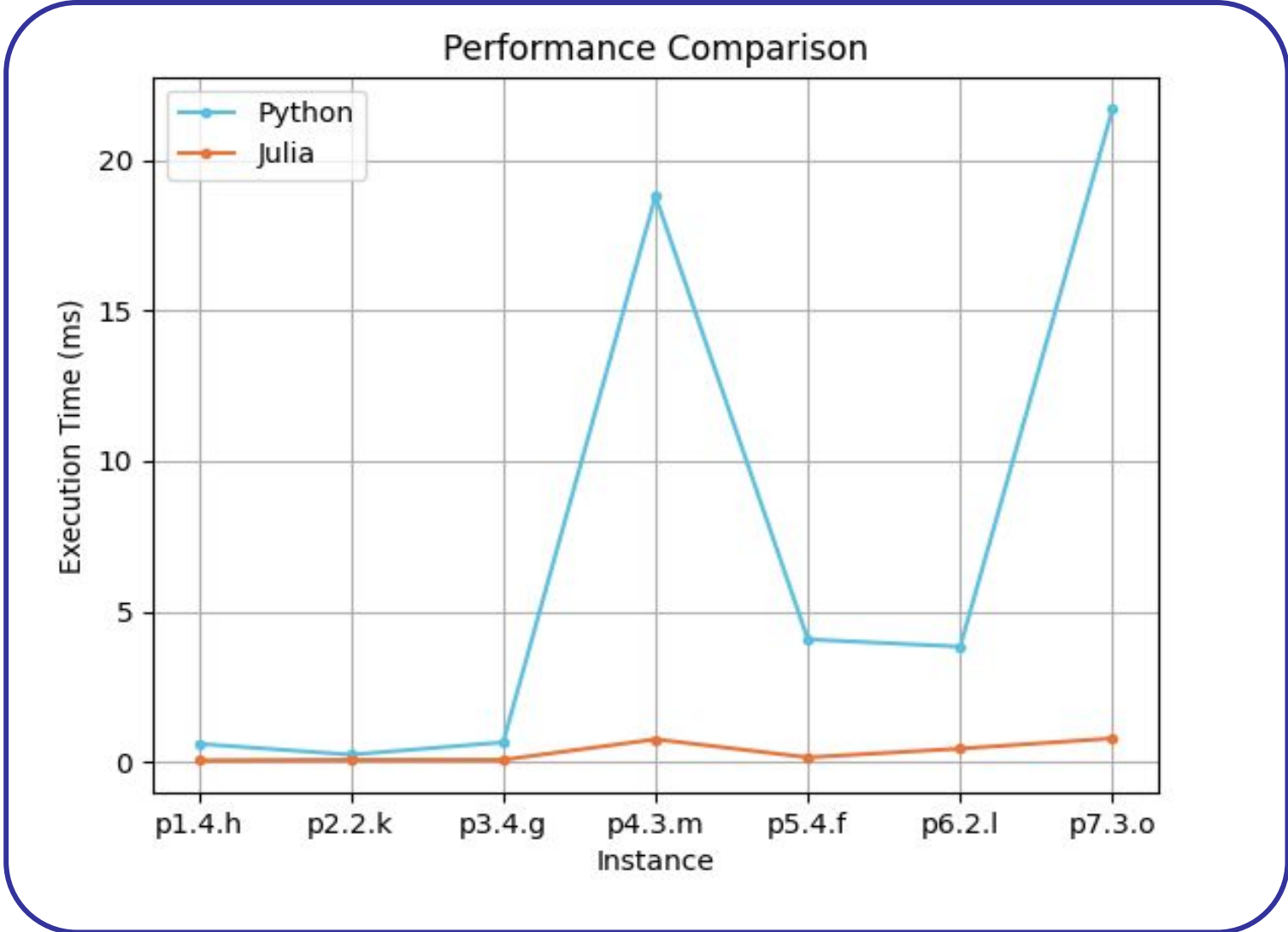
- The runtime for each instance was **measured from the start of the algorithm** to the moment the **final solution** was produced
- The **PJS heuristic** algorithm has been implemented using **Python 3.10**, and **Julia 1.8.2**
- Tested on a workstation with a multi-core processor **Intel Xeon E5-2630 v4** and **32 GB of RAM**

# Benchmark Process (II)

Instance	Python			Julia			Speedup
	Avg. Time	Min. Time	Max. Time	Avg. Time	Min. Time	Max. Time	
p1.4.h	0.60	0.58	0.82	0.05	0.05	0.09	11.0
p2.2.k	0.24	0.23	0.35	0.07	0.06	0.07	3.5
p3.4.g	0.65	0.63	0.86	0.07	0.07	0.14	8.7
p4.3.m	18.80	18.21	21.52	0.75	0.71	0.84	25.1
p5.4.f	4.07	3.96	5.02	0.15	0.14	0.17	26.9
p6.2.l	3.83	3.72	4.73	0.44	0.42	0.44	8.7
p7.3.o	21.69	21.09	27.31	0.78	0.74	0.83	27.8
Average:	7.13	6.92	8.66	0.33	0.31	0.37	16.0

- Execution time of Julia implementation is an order of magnitude faster
- Most challenging instances offer the most speedup gains
- Across all instances tested, the Julia implementation delivers an average speedup factor of 16x

# Benchmark Process (II)



## **Part IV:**

# **Conclusions and Future Directions**

# Conclusions



- **Powerful programming language** for solving routing problems
- Offers a **gentle learning curve** for Python users
- **Notable performance gains** achieved through compiler optimizations



# Future Directions

## Julia 1.9 Highlights



9 May 2023 | [The Julia contributors](#)

After 3 betas and 3 release candidates, Julia version 1.9 has finally(!) been released. We would like to thank all the contributors to this release and all the testers that helped with finding regressions and issues in the pre-releases. Without you, this release would not have been possible.

The full list of changes can be found in the [NEWS file](#), but here we'll give a more in-depth overview of some of the release highlights.

1. [Caching of native code](#)
2. [Package extensions](#)
3. [Heap snapshot](#)
4. [Memory usage hint for the GC with --heap-size-hint](#)
5. [Sorting performance](#)
6. [Tasks and the interactive thread pool](#)
7. [REPL](#)
  1. [Contextual module REPL](#)
  2. [Numbered prompt](#)
8. [DelimitedFiles](#) – first stdlib to be upgradable

## Python 3.12: A Game-Changer in Performance and Efficiency

Exploring the Exciting New Additions, Updates, and Changes in Python 3.12



AI TutorMaster · Follow

Published in Python in Plain English · 7 min read · Feb 14



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*Python 3.12, the latest version of the Python programming language, is expected to bring major optimizations and improvements to the language, with a focus on enhancing the speed, performance, and stability of the interpreter. This new release is designed to make Python a more powerful and efficient tool for developers, particularly for large and complex applications.*

**Improved Multi-Threaded Parallelism**

Mojo  – the  
programming language  
for all AI developers .

Mojo combines the usability of Python with the performance of C, unlocking unparalleled programmability of AI hardware and extensibility of AI models.



**Thank you for your attention!**

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